

# *Demystifying the hybrid coupler*



Picture: 4-squares at NR5M

by ON4UN

# *Demystifying the hybrid coupler*

## ■ Let's define the **Operational Bandwidth** Criteria for a directional array:

- **Gain:** constant +/- 0.5 dB
- **F/B:** min 20 dB over entire band
- **SWR:** max 1.8/1 at band edges

If 4-square array fed with a hybrid coupler we add:

- **Power dump:** min 10 dB at band edges

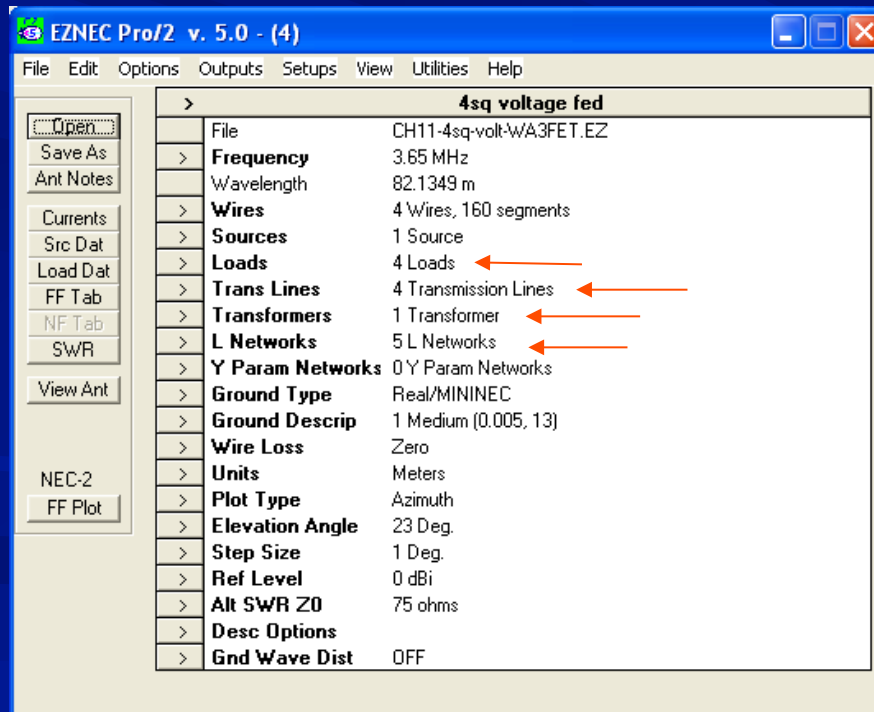
# *Demystifying the hybrid coupler*

- Ways of assessing the **Operational Bandwidth**:
  - through antenna **modeling**
  - or by **measuring**

# Demystifying the hybrid coupler

## “Antenna System” Modeling

- EZNEC modeling software can now incorporate feed lines, L, C, R, transformers etc.



This means we can include all the components of our LC network fed **ANTENNA SYSTEM** in the mathematical model

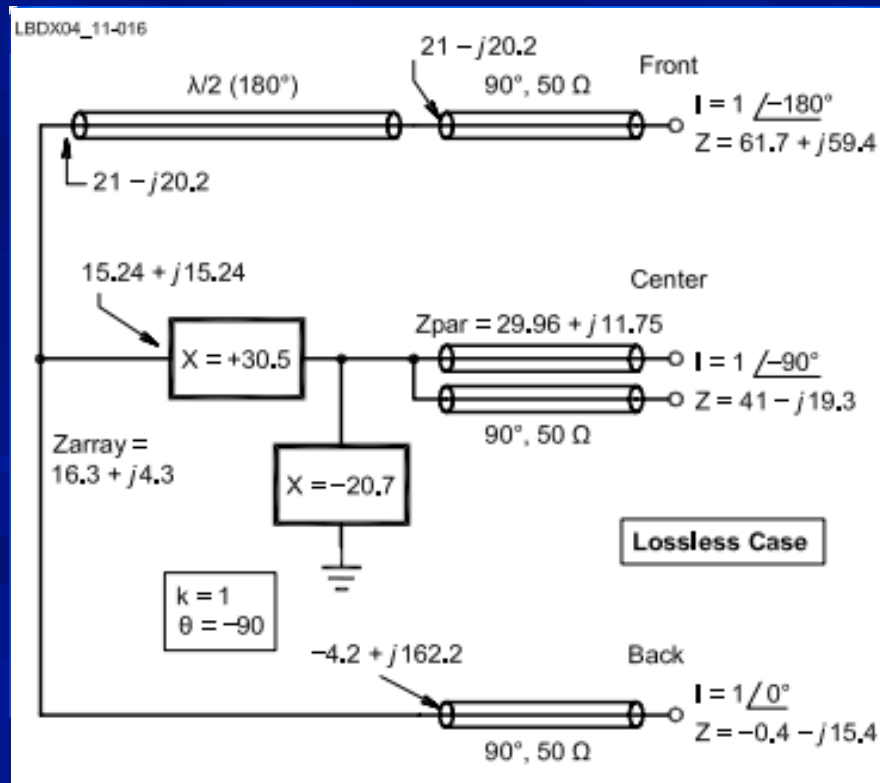
...and run the model across the band (using the **EZNEC sweep function**)...

to assess its performance

# Demystifying the hybrid coupler

## “Antenna System” Modeling

- EZNEC modeling software can now incorporate feed lines, L, C, R, transformers etc.



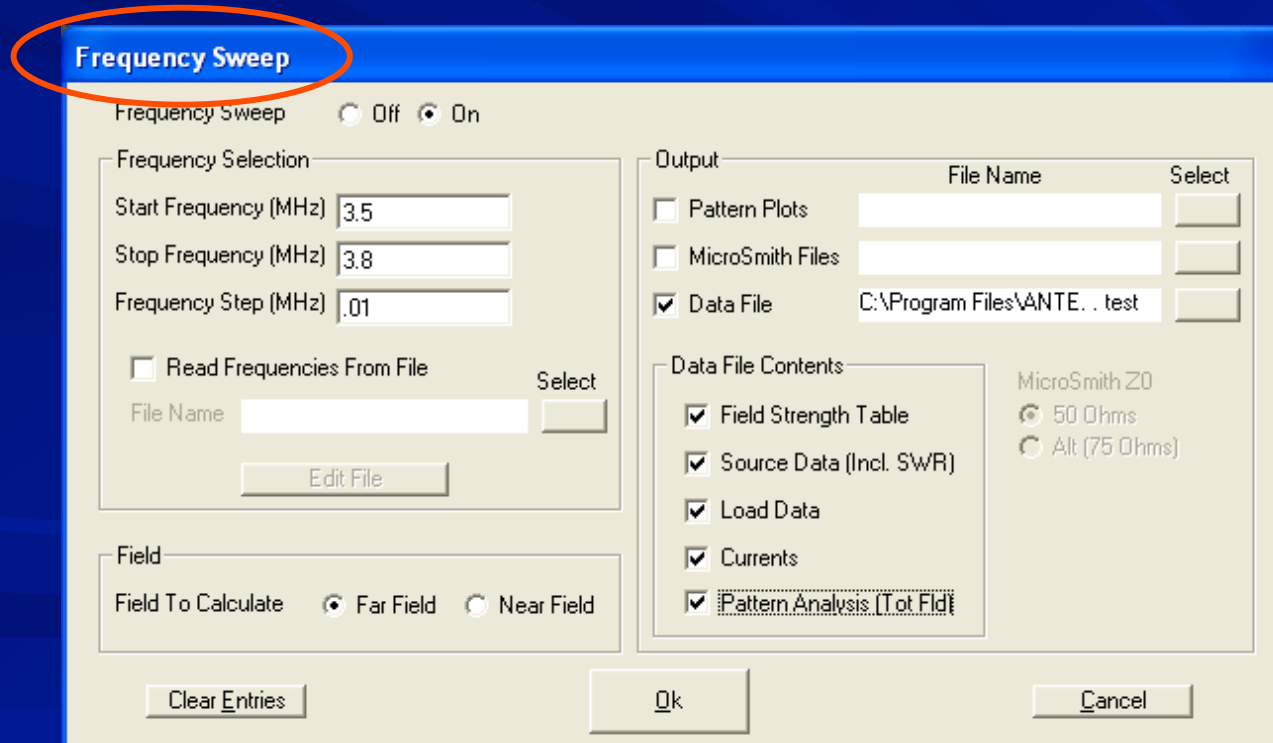
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...and run the model across the band (using the **EZNEC sweep function**)...

to assess its performance

# Demystifying the hybrid coupler

- EZNEC modeling software incorporates a **frequency sweep** function



# Demystifying the hybrid coupler

- The EZNEC modeling software creates a .txt file with all data in selected frequency steps

```

EZNEC Pro/2 ver. 5.0
2el-end-fire quad +feedlines          3/25/2010

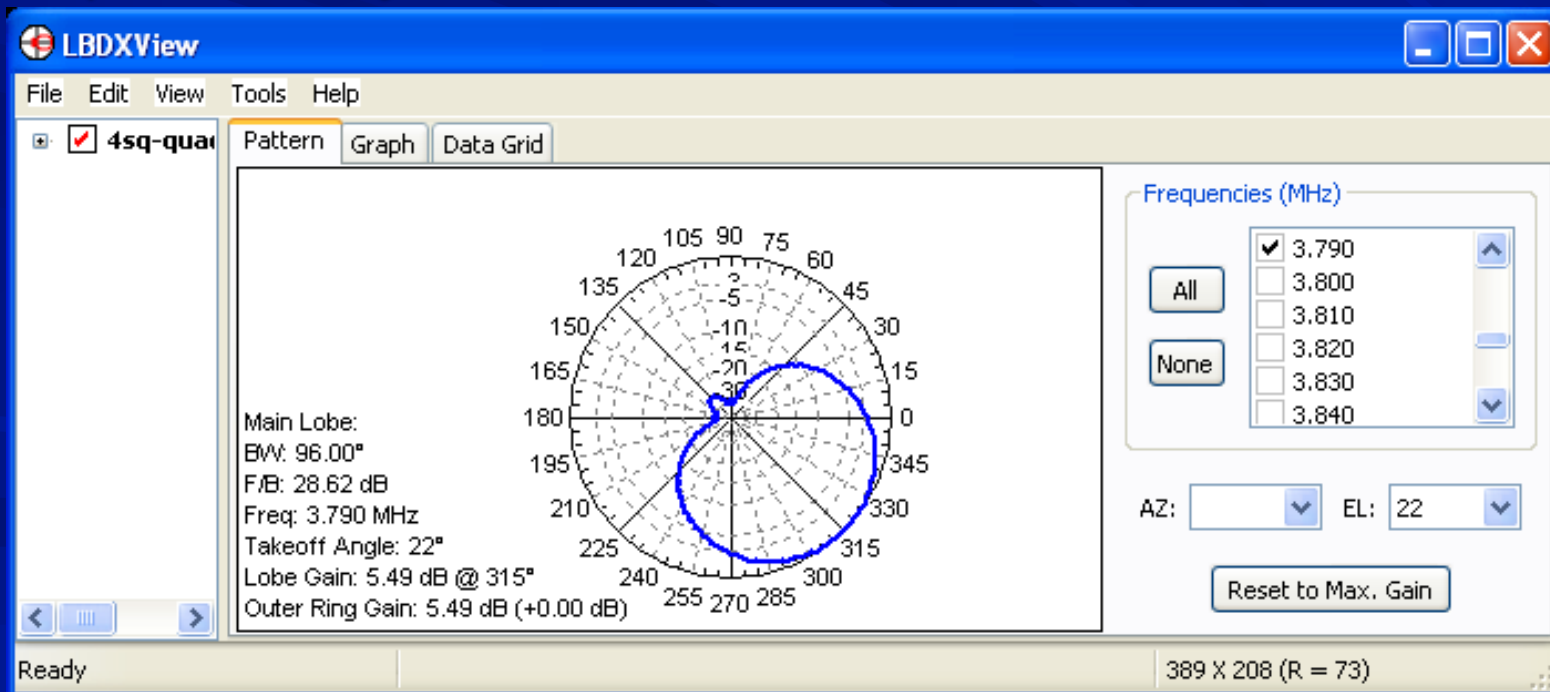
----- FAR FIELD PATTERN DATA -----
Frequency = 3.5 MHz
Reference = 0 dBi

Azimuth Pattern      Elevation angle = 23 deg.
Deg      V dB      H dB      Tot dB      V Pha      H Pha
0        2.93     -99.99     2.93     120.28     0.00
1        2.93     -99.99     2.93     120.27     0.00
2        2.93     -99.99     2.93     120.25     0.00
3        2.92     -99.99     2.92     120.22     0.00
4        2.92     -99.99     2.92     120.18     0.00
5        2.91     -99.99     2.91     120.13     0.00
6        2.90     -99.99     2.90     120.07     0.00
7        2.89     -99.99     2.89     119.99     0.00
8        2.88     -99.99     2.88     119.91     0.00
9        2.86     -99.99     2.86     119.81     0.00
10       2.85     -99.99     2.85     119.70     0.00
11       2.83     -99.99     2.83     119.58     0.00
12       2.81     -99.99     2.81     119.45     0.00
13       2.79     -99.99     2.79     119.31     0.00
14       2.77     -99.99     2.77     119.16     0.00
15       2.74     -99.99     2.74     118.99     0.00
16       2.72     -99.99     2.72     118.82     0.00
17       2.69     -99.99     2.69     118.63     0.00
18       2.66     -99.99     2.66     118.44     0.00
19       2.62     -99.99     2.62     118.23     0.00
20       2.59     -99.99     2.59     118.01     0.00
21       2.55     -99.99     2.55     117.78     0.00

```

# Demystifying the hybrid coupler

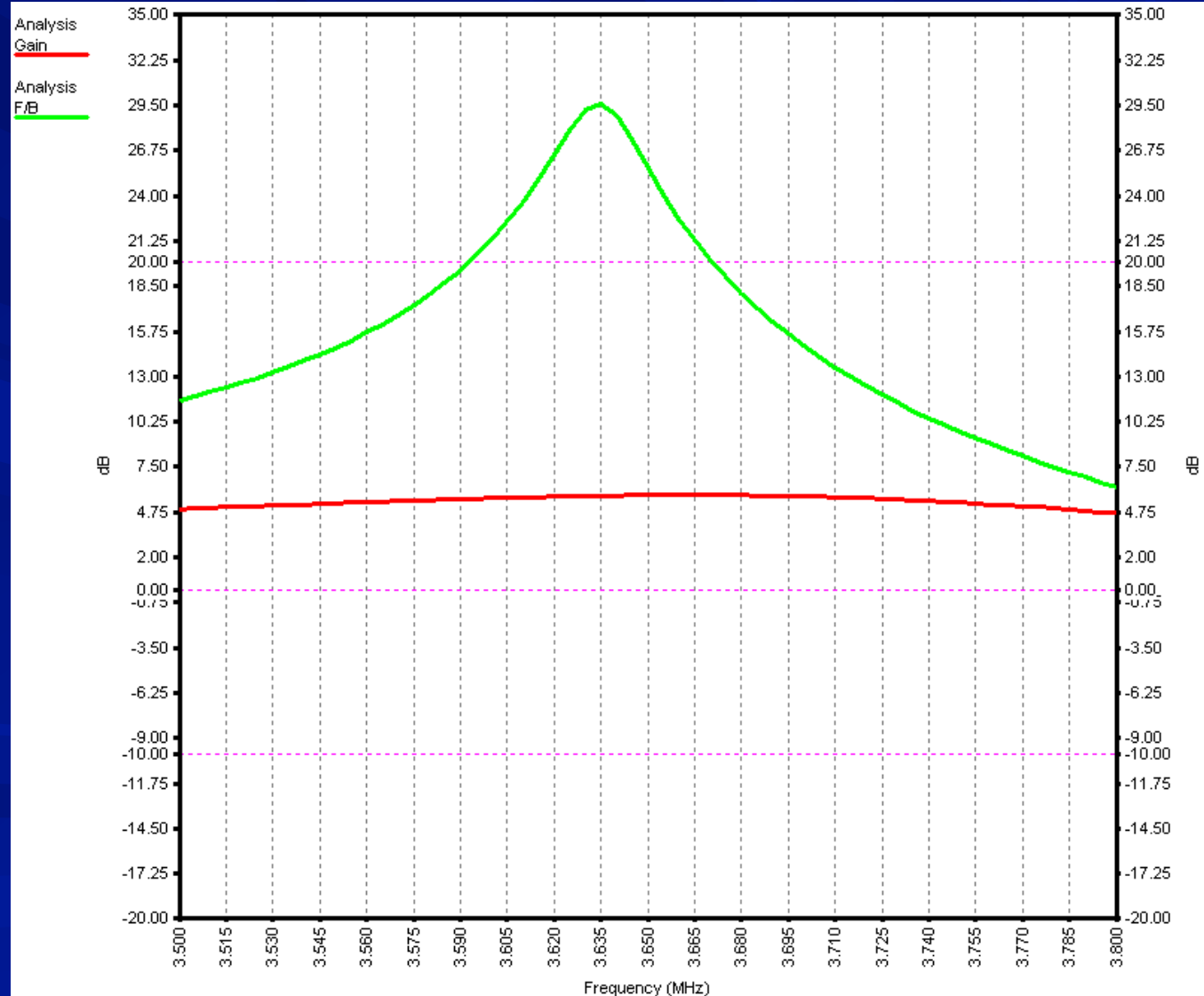
- The EZNEC modeling software creates a .txt file with all data in selected frequency steps...
- ...which can be used as input to **LBDXView** (written by **W8WWV**, available on the book's CD)





# Demystifying the hybrid coupler

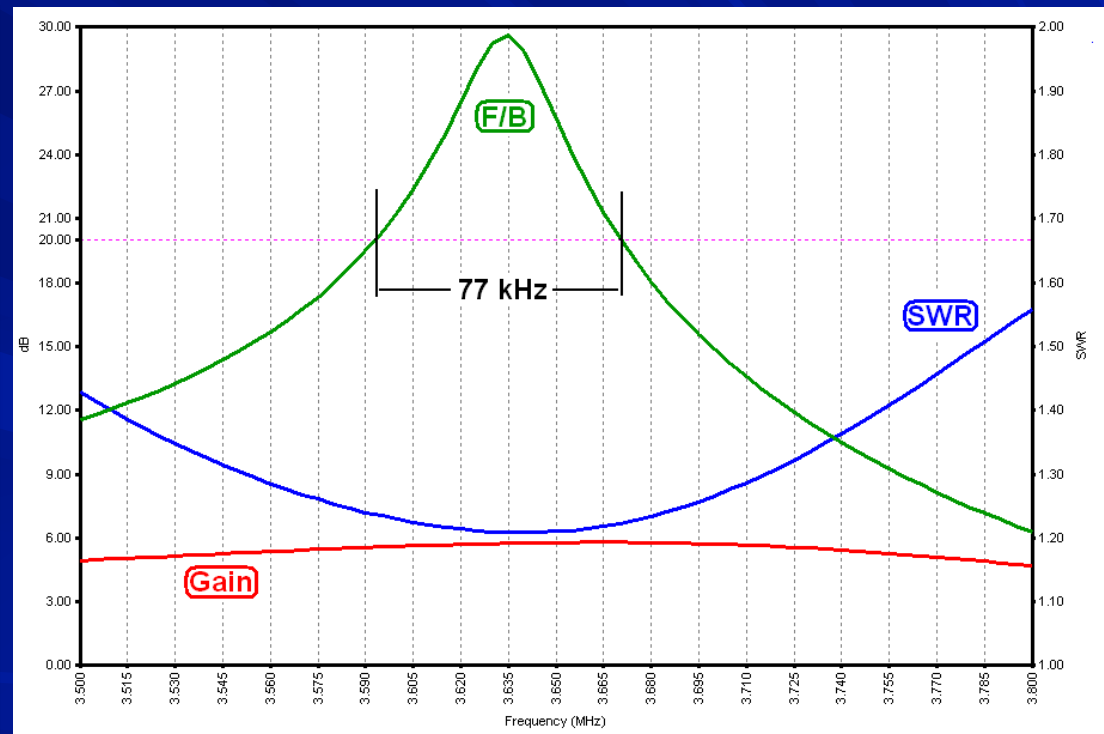
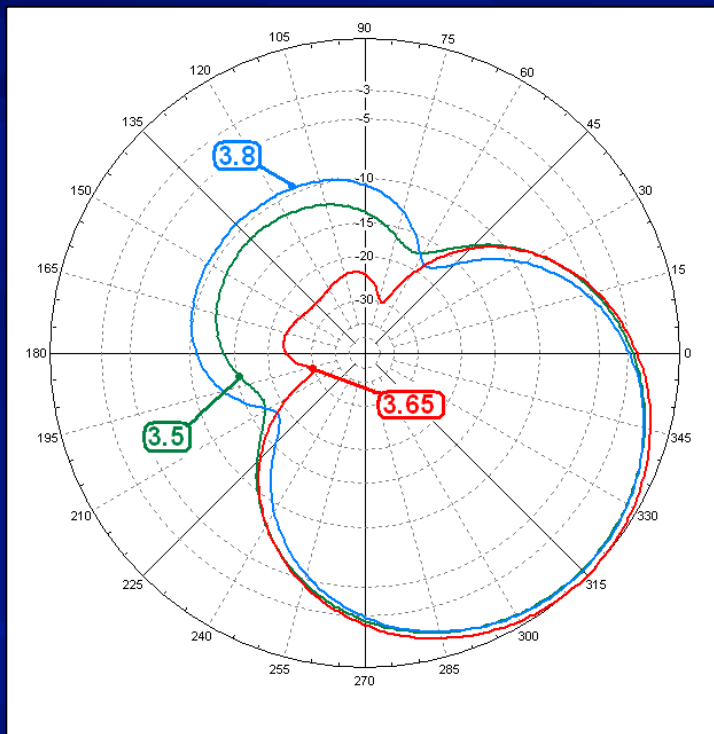
**LBDXView**



Gain and  
F/B Bandwidth

# Demystifying the hybrid coupler

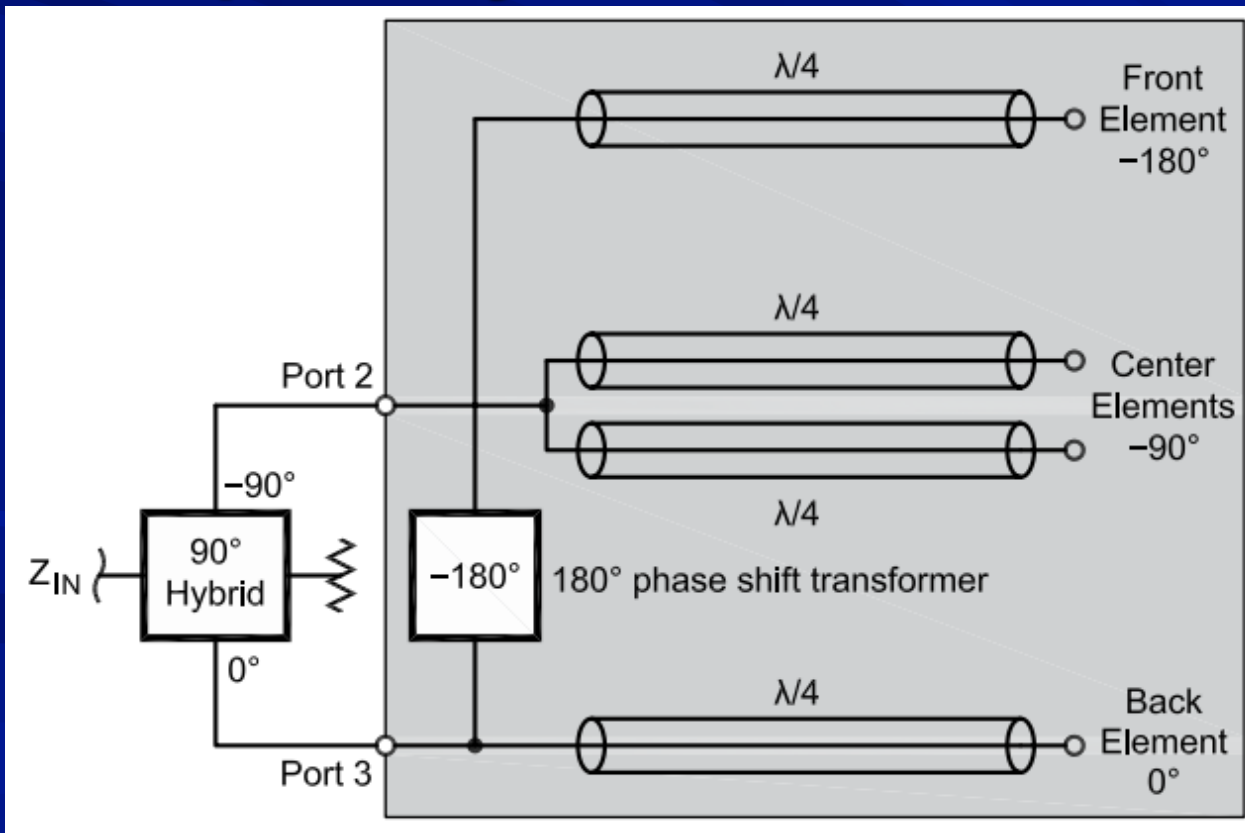
## L-network fed 4-square



**Conclusion: Operational Bandwidth <<<**

# Demystifying the hybrid coupler

- Let's look at the **hybrid coupler** fed 4-square system



# *Demystifying the hybrid coupler*

- Let's run a model in sweep mode
- Remember, model must include **ALL components** of the array (= the entire system)

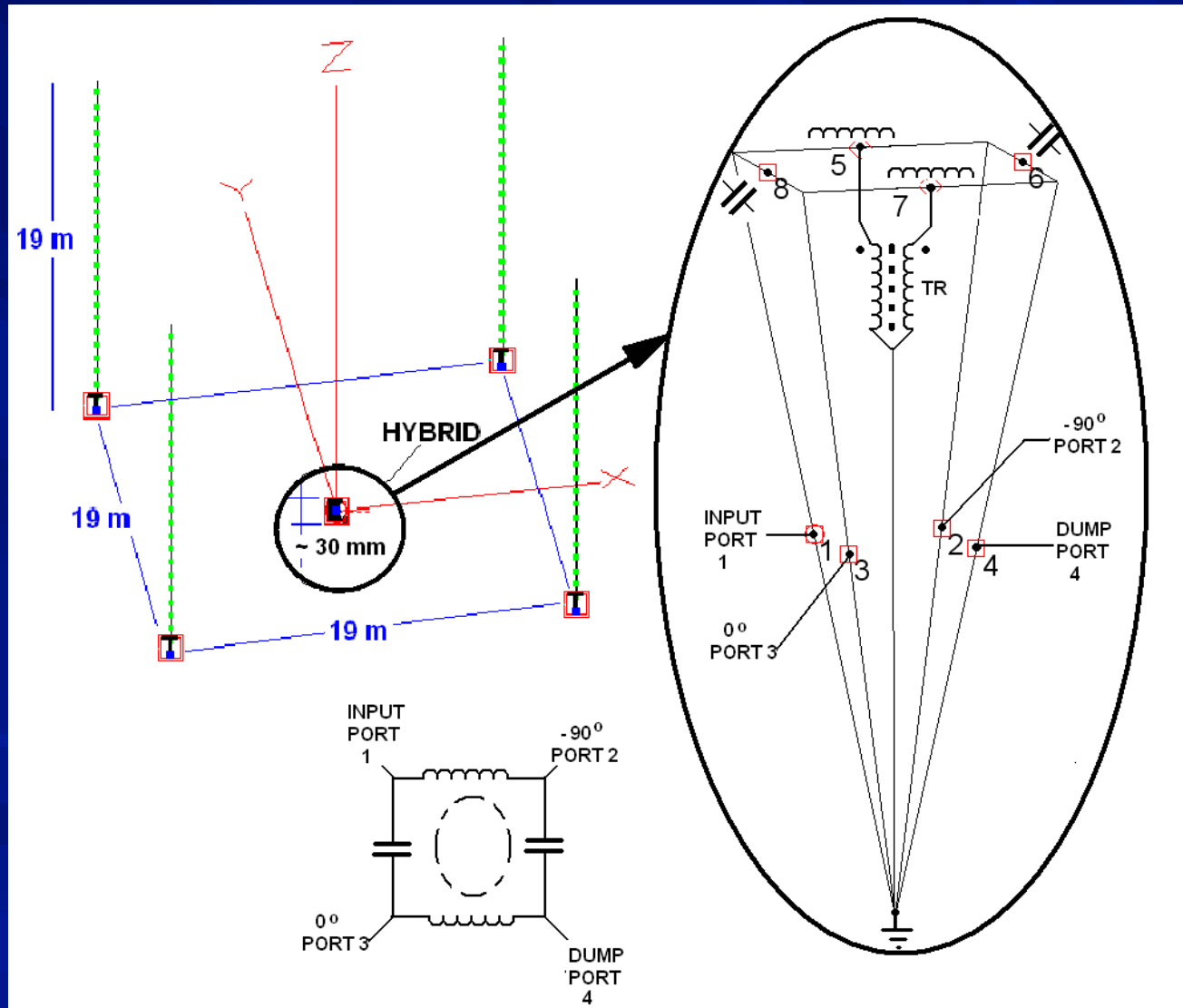
**That means the hybrid coupler also should be included in the model !**

# *Demystifying the hybrid coupler*

Until now a **hybrid** was **NEVER** included in an **antenna model**

- **W7EL** simply included the wiring of the hybrid (components and connections) in the center of the array at ground level
- Height of the construction:  $< 3 \text{ mm}$  ( $\sim 0.1 \text{ inch}$ )
- Hence: the wires radiate little or **NOTHING**

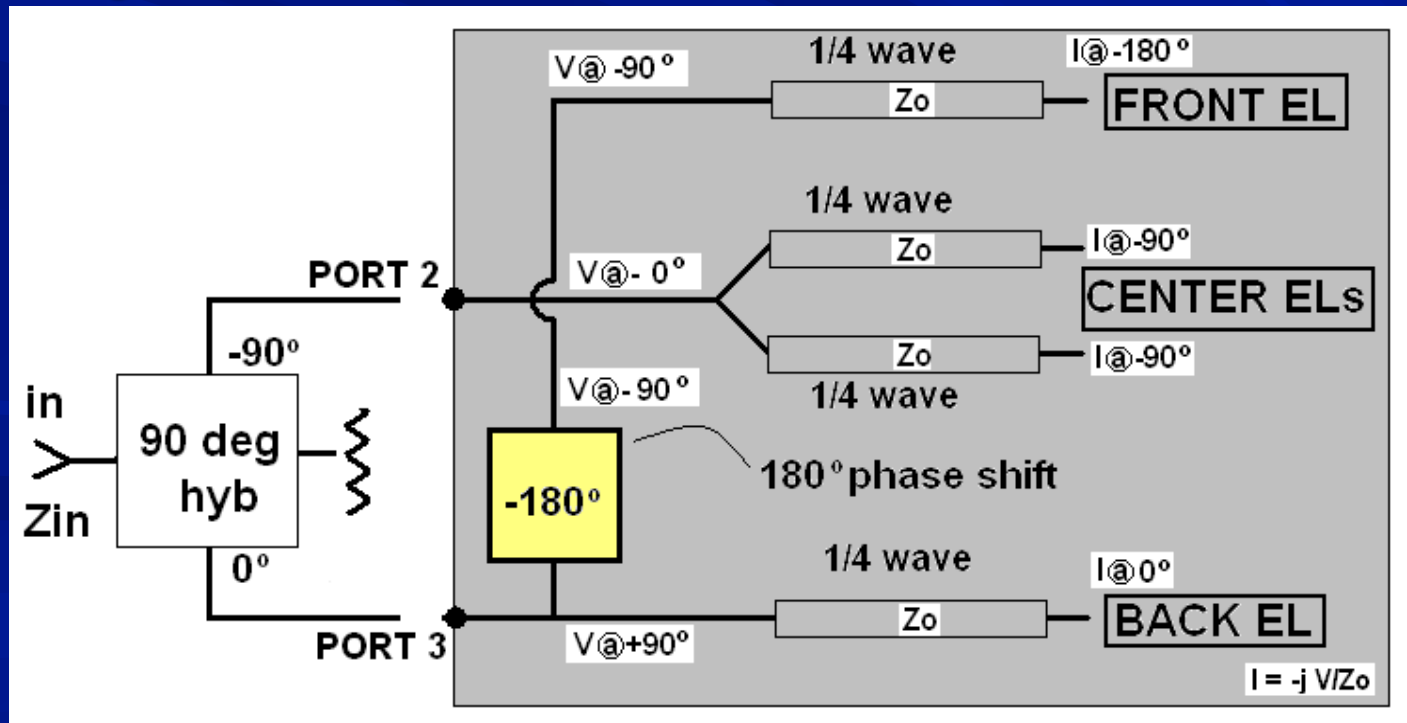
# Demystifying the hybrid coupler



# Demystifying the hybrid coupler

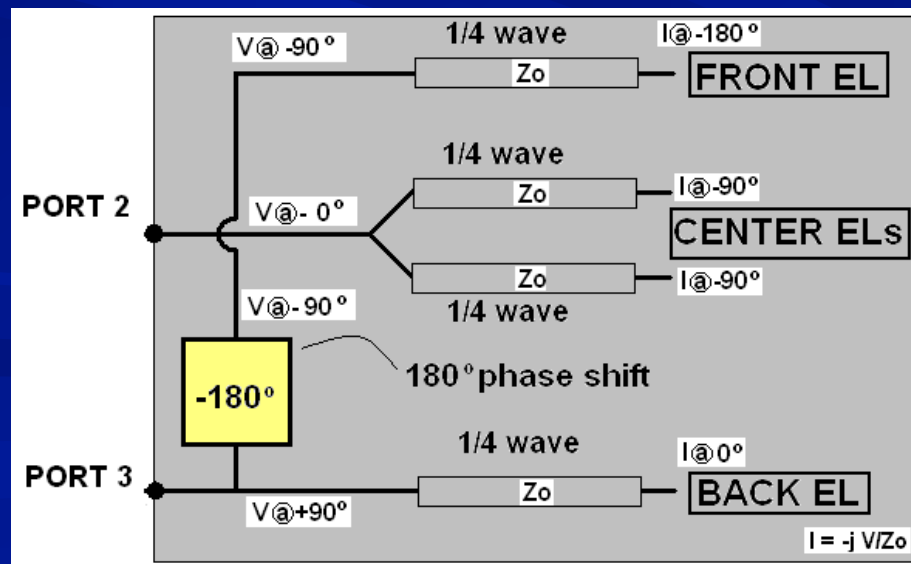
## THE FOUR-SQUARE BLACK BOX

- In order to simplify the analysis, W1MK suggested we reduce the 4-square to a 2-port **black box** and the **hybrid**



# Demystifying the hybrid coupler

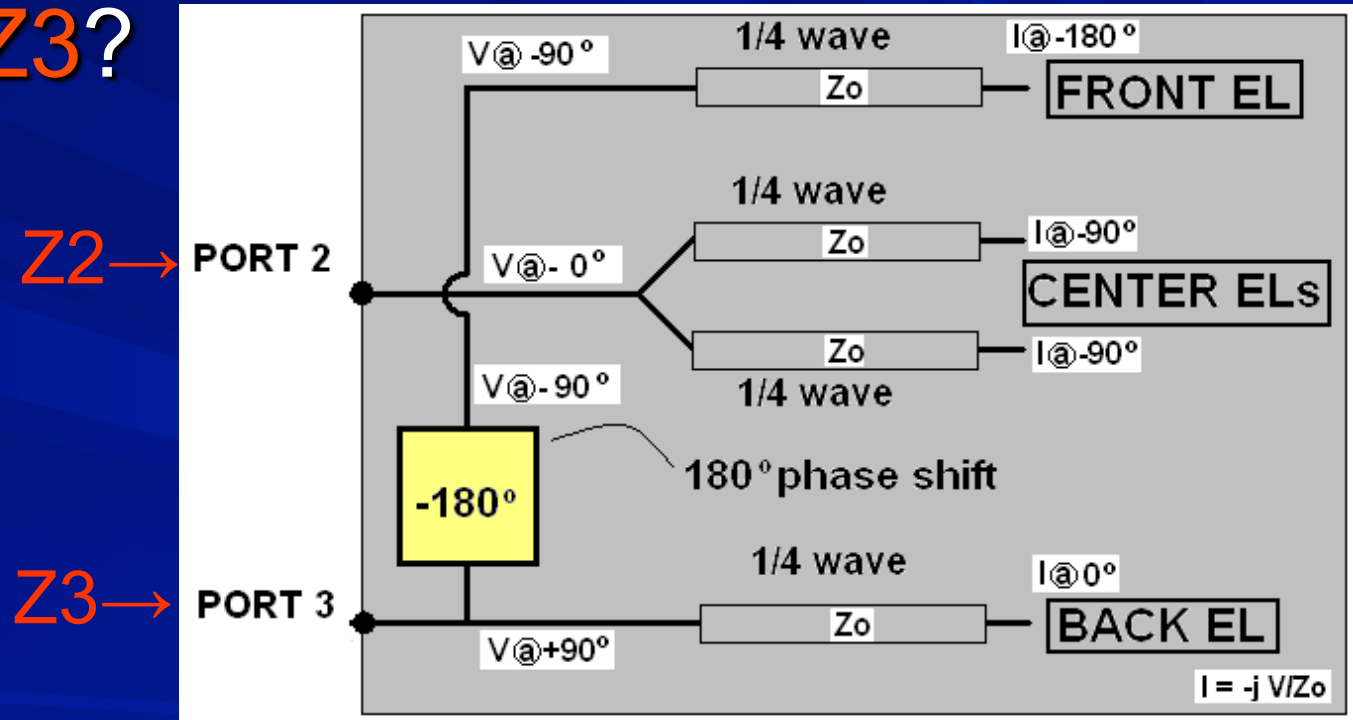
- W1MK noticed for the  $-90^\circ/-180^\circ$  4-square that if the 4-sq is electrically and physically well balanced
- ...there is **NO** effect on the impedance at one of these two ports, caused by changes at the other port. The 2 ports are independent and not coupled





# Demystifying the hybrid coupler

What are the VALUES of impedances **Z2** and **Z3**?



These can be modeled or measured

# Demystifying the hybrid coupler

## ■ THROUGH MODELING

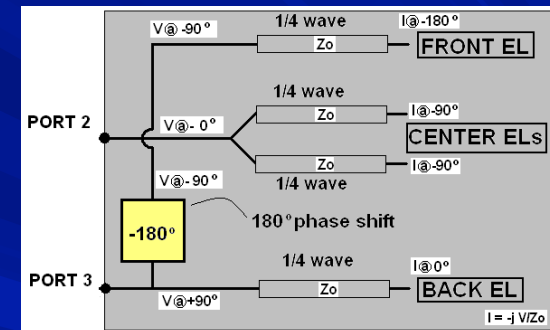
- Can easily be modeled, all black box components can be incorporated in an EZNEC model

Transmission Lines						
Wire #	% From E1	% From E1	Wire #	% From E1	% From E1	Z0
2	50	50	9	0	2	75
2	50	50	10	0	2	75
3	50	50	11	0	2	75
V6			12	0	2	75

Transformers						
No.	Port 1 Specified	Port 1 Act	Port 2 Specified	Port 2 Act	Port 1	Port 2
1	Wire #	% From E1	Wire #	% From E1	RelZ	
	V6		V2		50	

$$Z2 = 53.7 + j22.5$$

$$Z3 = 60.7 - j36.1$$



Frequency = 3.65 MHz

Source 1  
 Voltage = 0.852 V at -82.7 deg.  
 Current = 0.01463 A at 185.44 deg.  
 Impedance = 53.69 + J 22.51 ohms  
 Power = 0.0115 watts  
 SWR (50 ohm system) = 1.548 (75 ohm system) = 1.622

Source 2  
 Voltage = 1 V at 0.0 deg.  
 Current = 0.01417 A at 30.71 deg.  
 Impedance = 60.68 - J 36.05 ohms  
 Power = 0.01218 watts  
 SWR (50 ohm system) = 1.954 (75 ohm system) = 1.764

Total applied power = 0.02368 watts

# *Demystifying the hybrid coupler*

## ■ THROUGH **MEASURING**

**Case 1: perfectly symmetrical array** (physical and electrical symmetry)

- Remember there is no effect at either port 2 or port 3 caused by changes at the other port

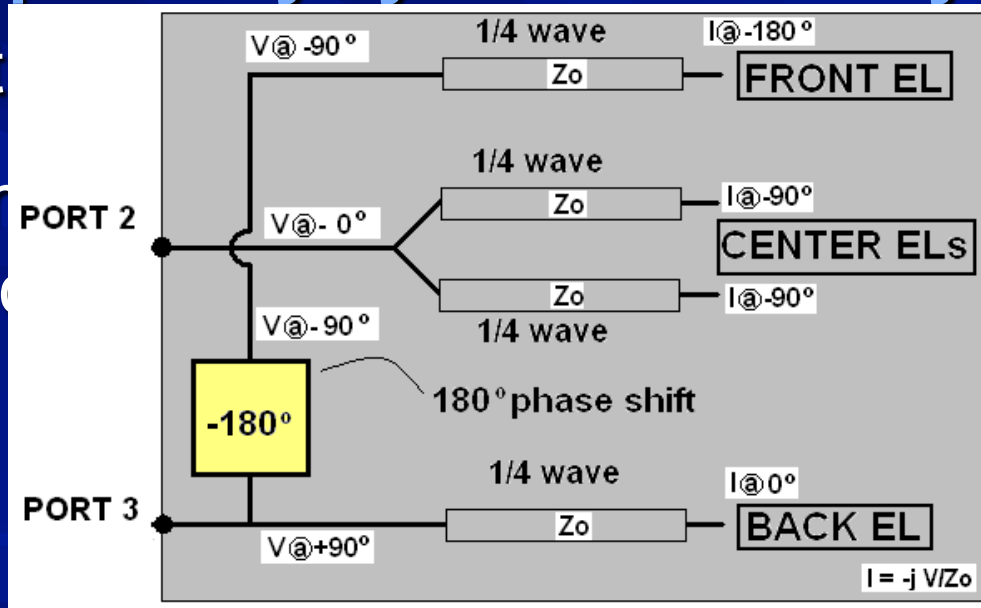
# Demystifying the hybrid coupler

## THROUGH MEASURING

Case 1: perfectly symmetrical array (physical

and elect

– Remember  
port 3



port 2 or  
port

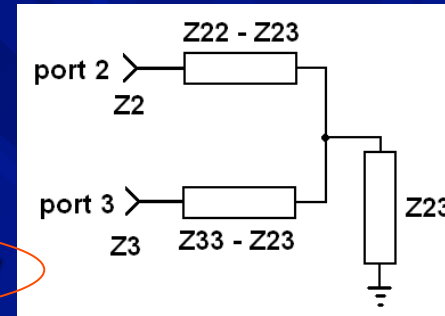
– Which means we can simply measure  $Z_2$  and  $Z_3$  at ports 2 and 3 of the black box

# Demystifying the hybrid coupler

## ■ THROUGH MEASURING

### Case 2: non symmetrical array

- USE SPREADSHEET PROGRAM (“2 port coupling”) on the book’s CD
- Measure  $Z_2$  with  $Z_3$  open  $\rightarrow Z_{22}$
- Measure  $Z_3$  with  $Z_2$  open  $\rightarrow Z_{33}$
- Measure  $Z_2$  with  $Z_3$  shorted  $\rightarrow Z_{2,3}$  ( $Z_{2,3}$  = coupled impedance)
- The program calculates  $Z_{23}$  (mutual impedance)
- Measuring of  $Z_2$  and  $Z_3$  in parallel is required to determine the sign of  $Z_{23}$  (re: square root)
- Program calculates  $Z_2$  and  $Z_3$
- ...and also “diagonal isolation” in dB



BLACK BOX 2-PORT COUPLING (W1MK)			
<b>A - INPUTS</b>			
1	Enter k $\rightarrow$	1	must be $\leq 1$
2	Enter Angle $\theta$ $\rightarrow$	90	must be -
		real part	imag part
3	Enter $Z_{22}$ $\rightarrow$	93.93	44.26
4	Enter $Z_{33}$ $\rightarrow$	123.1	94.99
5	Enter $Z_{2,3}$ $\rightarrow$	91.05	42.04
6	Enter Zin parr $Z_2+Z_3$ . $\rightarrow$	43	21
<b>B - CHOICE OF SIGN MUTUAL IMPEDANCE</b>			
7	$Z_{23} =$	18.83	14.52
8	IF Zin parr =	63.58	38.01
<b>OR</b>			
9	$Z_{23} =$	-18.83	-14.52
10	IF Zin parr =	44.68	24.75
11	Enter $Z_{23}$ $\rightarrow$	-18.83	-14.52
<b>C - OUTPUTS</b>			
12	$Z_2 =$	95.25	27.47
13	$Z_3 =$	91.39	106.04
<b>DIAGONAL ISOLATION</b>			
14	Diagonal Isolation =	-21.0 dB	

# *Demystifying the hybrid coupler*

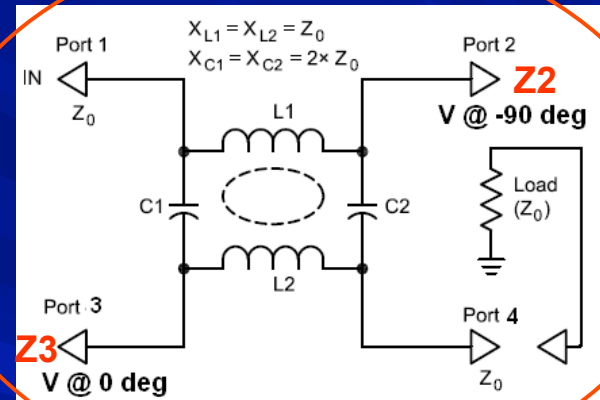
Now we know **Z2** and **Z3** (through modeling or via measuring)

- Will the hybrid coupler deliver voltages at ports 2 and 3 that are  $90^\circ$  out of phase (with same magnitude) for **any value** of Z2 and Z3?
- Obviously not!
- So what does it deliver?
- **...and what can we do so it does deliver what we want?**

# Demystifying the hybrid coupler

## The what and the how of the Hybrid

- Let's analyze the “mysterious” lumped coupled  $90^\circ$  hybrid
- Required split (being  $k=1$  and  $\theta=90^\circ$ ) occurs **only if Z2 and Z3 have specific relationship**
  - Which relationship?
- To be able to answer those questions W1MK developed a **mathematical model** for the hybrid coupler (a first!)



# Demystifying the hybrid coupler

## MATHEMATICS 90° LUMPED ELEMENT HYBRID COUPLER

By Robye L. Lahlum, W1MK

### Port 1 Terms

$$V_{IN} = V_1^+ + V_1^-$$

$$V_{IN} = V_1^+ (1 + \rho_{IN})$$

$V_1^+ \rightarrow$  forward voltage (incident voltage)

$V_1^- \rightarrow$  reflected voltage

### Adjacent Ports Transfer Functions

$$A = \sqrt{\frac{f_o}{f_a}} \angle \theta_1$$

$$B = \sqrt{\frac{f_o}{f_a}} \angle \theta_2$$

$\rho_{IN}, \rho_2, \rho_3$  and  $\rho_4$  are reflection coefficients and in general complex, as are the variables  $Y$  and  $Z$

$f_o$  = center frequency of hybrid coupler

$f_a$  = operating frequency

$$\frac{V_2}{V_1^+} = 0.707 \cdot \sqrt{\frac{f_o}{f_a}} \cdot (1 + \rho_1) \cdot X \angle \theta_1 \quad (0.707 = \frac{\sqrt{2}}{2})$$

$$\frac{V_3}{V_1^+} = 0.707 \cdot \sqrt{\frac{f_o}{f_a}} \cdot (1 + \rho_1) \cdot Y \angle \theta_2 \quad (0.707 = \frac{\sqrt{2}}{2})$$

$$\frac{V_2}{V_3} = -j \sqrt{\frac{f_o}{f_a}} \frac{(1 + \rho_1) \cdot X}{(1 + \rho_1) \cdot Y}$$

$$\frac{V_4}{V_1^+} = \frac{(\rho_2 + \rho_3) \cdot Z}{2}$$

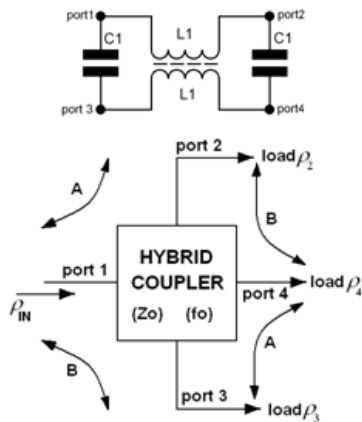
$$\frac{V_4}{V_1^+} = \rho_{IN} = \left[ \frac{\rho_2}{2} \left( \frac{f_o}{f_a} \right) \cdot X \right] \angle 2\theta_1 + \left[ \frac{\rho_3}{2} \left( \frac{f_o}{f_a} \right) \cdot Y \right] \angle 2\theta_2 = \rho_c + j\rho_i$$

$$\rho_{IN} = \rho_c + j\rho_i = \left[ \frac{\rho_2}{2} \left( \frac{f_o}{f_a} \right) \cdot X \right] \angle 2\theta_1 + \left[ \frac{\rho_3}{2} \left( \frac{f_o}{f_a} \right) \cdot Y \right] \angle 2\theta_2$$

$$Z_{IN} = \frac{1 - \rho_{IN}}{1 + \rho_{IN}} \cdot Z_o$$

$$R_{IN} = Z_o \cdot \frac{(1 - \rho_c^2 - \rho_i^2)}{(1 - \rho_c^2) + \rho_i^2}$$

$$X = \frac{2 \cdot Z_o}{(1 - \rho_c^2) + \rho_i^2}$$



where:

$$X = 1 + \left( \frac{f_o}{f_a} \right) \cdot \frac{(\rho_2 + \rho_3)}{2} \cdot \rho_1 \cdot [\cos(\theta_2 - \theta_1) + j \sin(\theta_2 - \theta_1)]$$

$$Y = 1 + \left( \frac{f_o}{f_a} \right) \cdot \frac{(\rho_2 + \rho_3)}{2} \cdot \rho_1 \cdot [\cos(\theta_2 - \theta_1) - j \sin(\theta_2 - \theta_1)]$$

$$Z = 1 + \rho_1$$

$$\theta_1 = -A \cdot \text{ATAN} \left( \frac{f_o}{f_a} \right) \text{ and } \theta_2 = A \cdot \text{ATAN} \left( \frac{f_o}{f_a} \right)$$

**Conversion** from  $\left( \frac{V_4}{V_1^+} \right) \angle \theta$   $\frac{\text{Power Out Port4}}{\text{Power In Port1}}$

$\rho_{IN}$  = reflection coefficient at input

$$V_{IN} = V_1^+ + V_1^- = V_1^+ \cdot (1 + \rho_{IN})$$

$$\rho_{IN} = \frac{V_1^-}{V_1^+} = \rho_c + j\rho_i$$

$$V_{IN}^2 = (V_1^+)^2 \cdot [(1 + \rho_c)^2 + (\rho_i)^2]$$

$$\text{Power In (Port1)} = \frac{V_{IN}^2}{R_{IN}}$$

$$R_{IN} = \frac{Z_o \cdot [(1 + \rho_c)^2 + (\rho_i)^2]}{(1 - \rho_c^2 - \rho_i^2)}$$

$$\frac{\text{Power Port4}}{\text{Power In}} = \frac{V_4^2}{V_{IN}^2} \cdot \frac{Z_o \cdot [(1 + \rho_c)^2 + (\rho_i)^2]}{R_{IN} \cdot (1 - \rho_c^2 - \rho_i^2)}$$

$$\frac{\text{Power Port4}}{\text{Power In}} = \frac{V_4^2}{(V_1^+)^2} \cdot \frac{Z_o}{R_{IN} \cdot (1 - \rho_c^2 - \rho_i^2)}$$

When  $\rho_i = 0$  (means: load port termination equals  $Z_o$ )

then:

$X=1, Y=1$  and  $Z=1$

and:

$$\frac{V_3}{V_1^+} = -j \left( \frac{f_o}{f_a} \right) \frac{(1 + \rho_1)}{(1 + \rho_1)}$$

$$\frac{V_4}{V_1^+} = \frac{(\rho_2 + \rho_3)}{2}$$

$$\frac{V_4}{V_1^+} = \rho_{IN} = \frac{\rho_2}{2} \left( \frac{f_o}{f_a} \right) \angle 2\theta_1 + \frac{\rho_3}{2} \left( \frac{f_o}{f_a} \right) \angle 2\theta_2$$

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# Demystifying the hybrid coupler

Based on these mathematics a hybrid circuit modeling tool was developed

$$\frac{V_2}{V_3} = -j \left( \frac{1 + \rho_2}{1 + \rho_3} \right) \left( \frac{f_o}{f_a} \right)$$

$$\text{Dump PWR} = [\dots] (\rho_2 + \rho_3)^2$$

$$\text{Refl. PWR} = [\dots] (\rho_2 - \rho_3)^2$$

HYBRID COUPLER DESIGN (by W1MK)			
<b>INPUTS</b>			
ENTER fa (operating frequency) →	3.65	MHz	
ENTER fo (hybrid frequency) →	3.65	MHz	
ENTER Zo Design impedance hybrid →	50	Ω	
	Real Part	Imag Part	
ENTER Impedance load PORT 2 (Z2) →	50	0	Ω
ENTER Impedance load PORT 3 (Z3) →	50	0	Ω
<b>RESULTS</b>			
fo/fa =	1.000		
Hybrid L value (uH) =	2.18	μH	
Hybrid C value (pF) =	436	pF	
Ratio Voltage magnitude Port2/Port3 (k) =	1.000		←
Phase angle Voltage port 2 vs. port 3 =	-90.00	°	←
Power in Port 4 (vs. Pwr in Port 1) =	∞	dB	←
Real part input impedance (port 1) =	50.00	Ω	
Imaginary part input impedance (port1) =	0.00	Ω	
Return loss (port 1) =	∞	dB	
SWR =	1.00		←

the modeling tool does all of the above calculations based on the load impedances **Z2** and **Z3**

**k** = voltage ratio (v2/v3)

# Demystifying the hybrid coupler

- For further calculations...
- ...we will take the Z2 and Z3 results from our EZNEC model

```
Frequency = 3.65 MHz

Source 1      Voltage = 0.852 V at -82.7 deg.
              Current = 0.01462 A at -105.44 deg.
              Impedance = 53.69 + J 22.51 ohms
              Power = 0.0115 watts
              SWR (50 ohm system) = 1.548 (75 ohm system) = 1.622

Source 2      Voltage = 1 V at 0.0 deg.
              Current = 0.01417 A at 38.71 deg
              Impedance = 60.68 - J 36.05 ohms
              Power = 0.01218 watts
              SWR (50 ohm system) = 1.954 (75 ohm system) = 1.764

Total applied power = 0.02368 watts
```

and use them in our calculations

# Demystifying the hybrid coupler

## RESULTS:

- $\Theta = -67^\circ$  (target:  $-90^\circ$ )
- $K = 0.9$  (target = 1)

## But ...

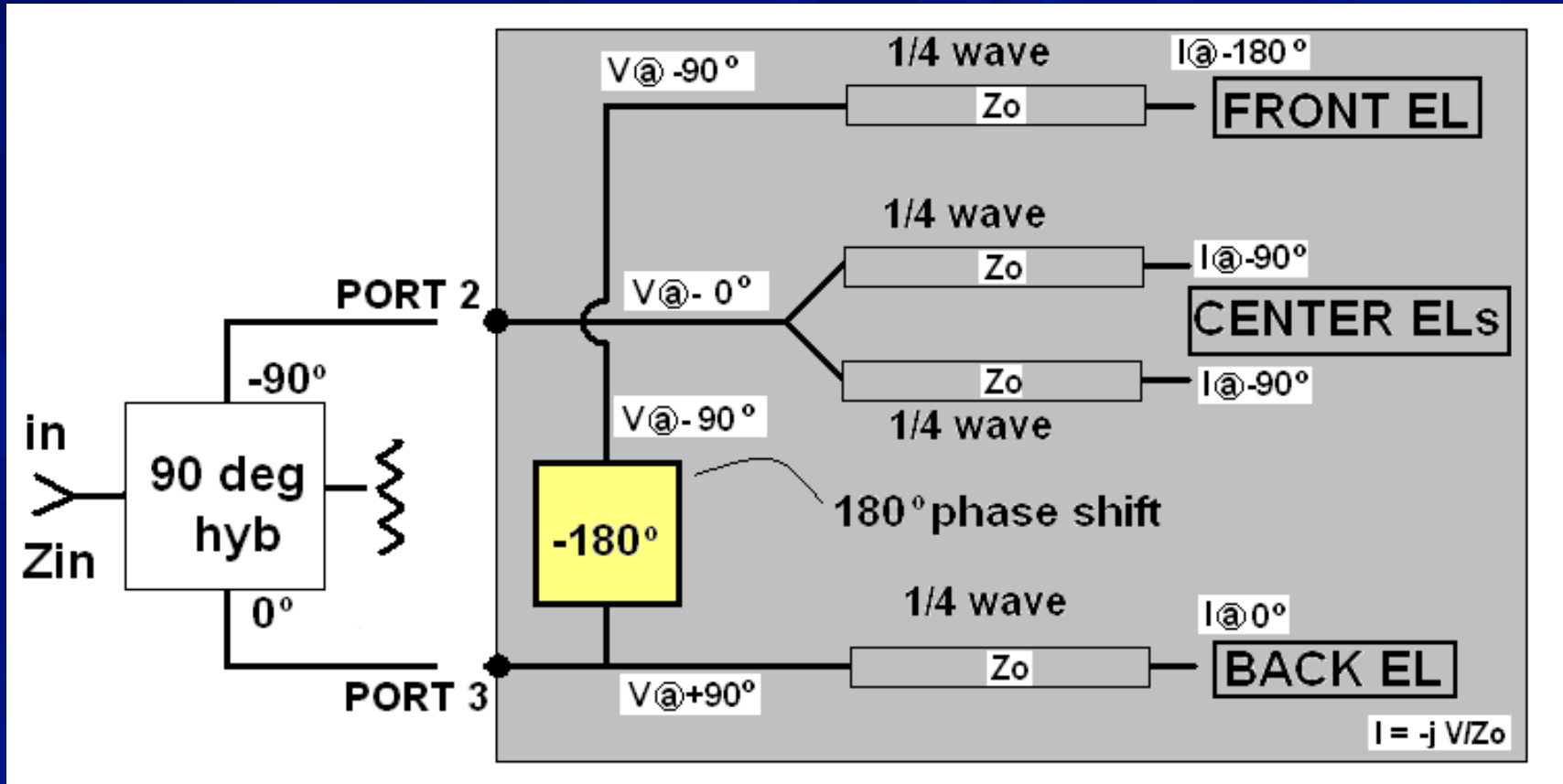
...there are ways to make  $k=1$  and  $\theta = 90^\circ$

HYBRID COUPLER DESIGN (by W1MK)			
<b>INPUTS</b>			
ENTER fa (operating frequency) →	3.65	MHz	
ENTER fo (hybrid frequency) →	3.65	MHz	
ENTER Zo Design impedance hybrid →	50	$\Omega$	
	Real Part	Imag Part	
ENTER Impedance load PORT 2 (Z2) →	53.7	22.5	$\Omega$
ENTER Impedance load PORT 3 (Z3) →	60.7	-36.1	$\Omega$
<b>RESULTS</b>			
fo/fa =	1.000		
Hybrid L value ( $\mu$ H) =	2.18	$\mu$ H	
Hybrid C value (pF) =	436	pF	
Ratio Voltage magnitude Port2/Port3 (k) =	0.905		
Phase angle Voltage port 2 vs. port 3 =	66.83	$^\circ$	
Power in Port 4 (vs. Pwr in Port 1) =	-17.1	dB	
Real part input impedance (port 1) =	79.78	$\Omega$	
Imaginary part input impedance (port1) =	8.84	$\Omega$	
Return loss (port 1) =	-12.4	dB	
SWR =	1.63		

REMEMBER WHAT'S IMPORTANT: THE DRIVE CURRENT AT THE BASE OF THE RADIATING ELEMENTS ...

...OR THE DRIVE VOLTAGE AT THE END OF THE CURRENT FORCING LINES GOING TO THE RADIATING ELEMENTS !

# Demystifying the hybrid coupler



**REMEMBER WHAT'S IMPORTANT: THE DRIVE CURRENT AT THE BASE OF THE RADIATING ELEMENTS ...**

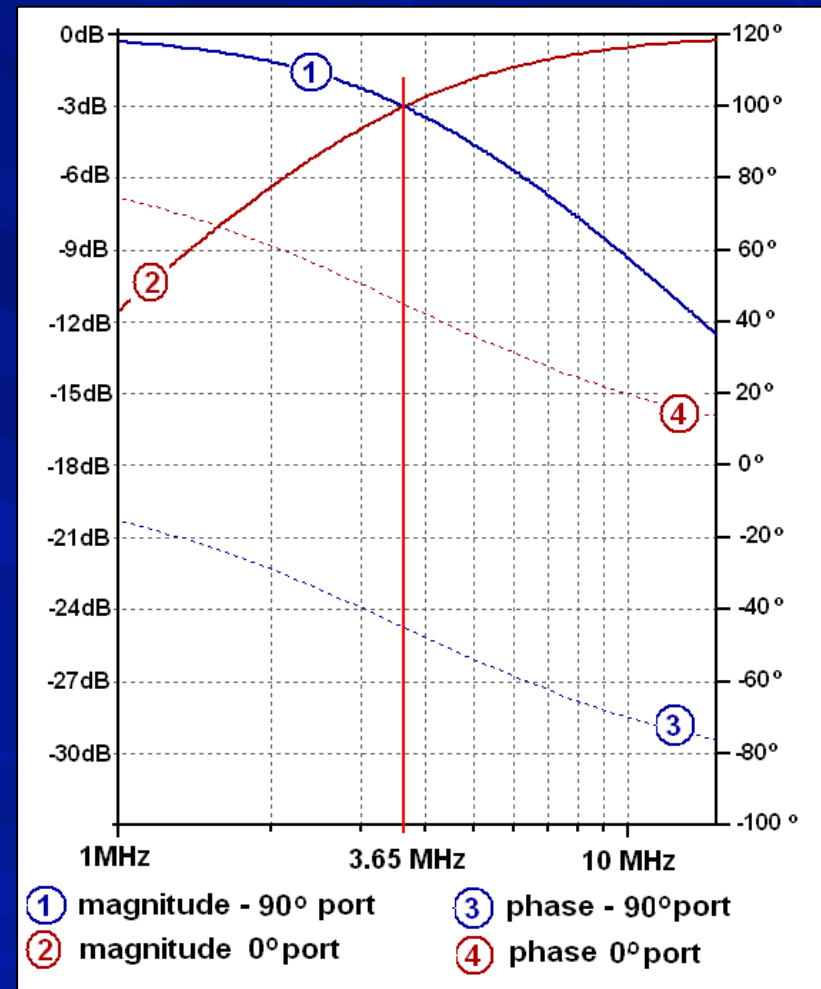
**...OR THE DRIVE VOLTAGE AT THE END OF THE CURRENT FORCING LINES GOING TO THE RADIATING ELEMENTS !**

# Demystifying the hybrid coupler

## Important special property of hybrid

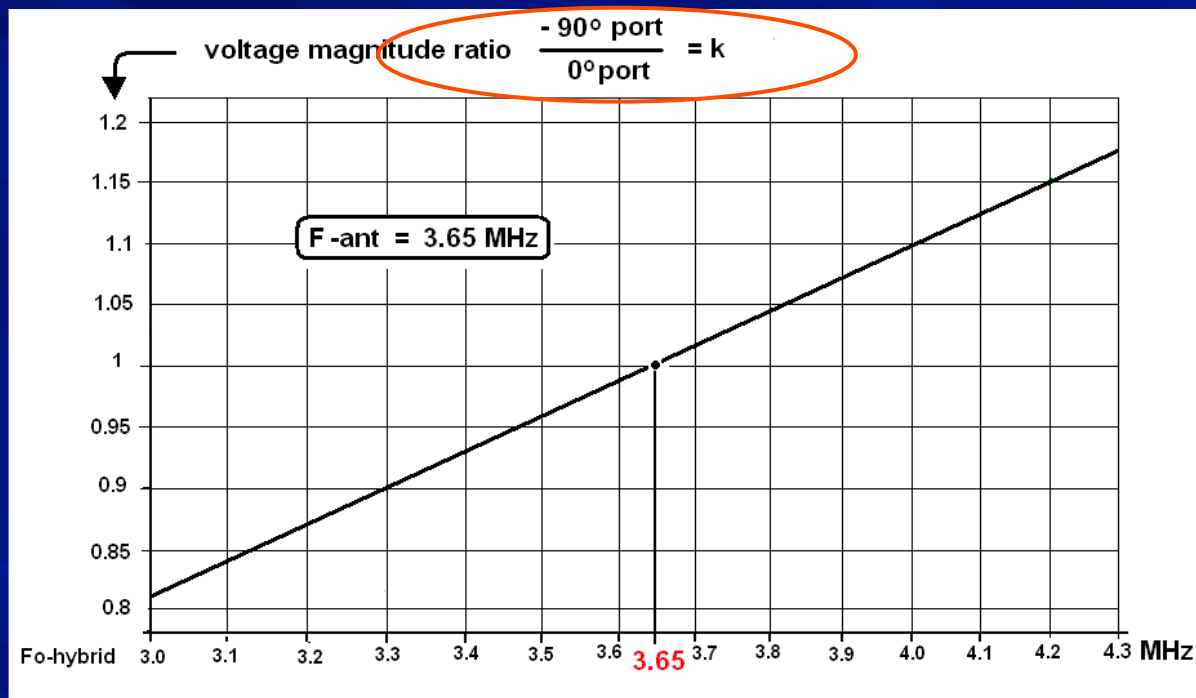
Voltage magnitude ratio ( $k = v_2/v_3$ ) can be changed by changing hybrid design frequency ( $Z_0$ ).

This unique property was first used by W8WWV in his “**Double network optimization**” approach, and has been the basis for the introduction of the other optimization systems for hybrid coupler feed systems. Thank you Greg!



# Demystifying the hybrid coupler

$k$  = ratio of voltage magnitude at port 2 vs. voltage magnitude at port 3



With **unequal resistive loads** ( $Z_2, Z_3$ ) we can obtain  $k=1$  by shifting the design frequency of the hybrid

Presented at Dayton 2008, by W8WWV

# *Demystifying the hybrid coupler*

What are the properties of the signals (at ports 2 and 3) that we want the hybrid to deliver?

- 90° phase shift
- identical voltage magnitude ( $k=1$ )

# Demystifying the hybrid coupler

Basic formula:

$$\frac{V_2}{V_3} = -j \left( \frac{1 + \rho_2}{1 + \rho_3} \right) \left( \frac{f_o}{f_a} \right)$$

calculated with Hybrid design spreadsheet

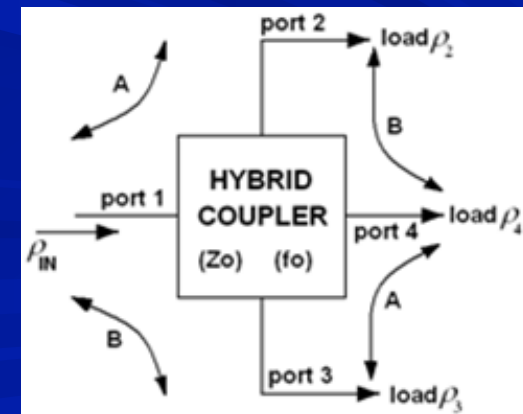
## ■ A few “special” cases

CASE	R2	X2	R3	X3	Zo	Port4	Port 1	k	$\theta$	fa	fo	remarks
1	50	0	50	0	50	$\infty$	$\infty$	1	-90	3.65	3.65	both 50 $\Omega$
2	68	0	68	0	50	-16.3	$\infty$	1	-90	3.65	3.65	identical real impedances
3	54	0	39	0	50	-27.2	-21.8	1.185	-90	3.65	3.65	different real impedances
4	54	0	39	0	50	-27.2	-21.8	1	-90	3.65	3.08	as above but with fo/fa compensation
5	33	10	33	10	50	-12.5	$\infty$	1	-90	3.65	3.65	identical complex impedances (matched mismatches)
6	53.7	22.5	60.7	-36	50	-17.1	-12.5	0.905	-66.8	3.65	3.65	random impedances

Note that there are a number of cases where  $\theta = -90^\circ$

Port 1:  $\rightarrow$  SWR (reflected PWR)

Port 4:  $\rightarrow$  dump power





# Demystifying the hybrid coupler

■ Let's look again at the 3 steps:

CASE	R2	X2	R3	X3	Zo	Port4	Port 1	k	$\theta$	fa	fo	remarks
12	53.7	22.5	60.7	-36	50	-17.1	-12.5	0.905	-66.8	3.65	3.65	
13	63.1	0	82.1	0	50	-14.9	-22.7	0.898	-90	3.65	3.65	add -150 $\Omega$ across Z2 and +138 $\Omega$ across Z3
14	63.1	0	82.1	0	50	-14.9	-27	1	-90	3.65	4.06	change fo to 4.06 MHz (k compensation)

This is the **W1MK 2-shunt method**

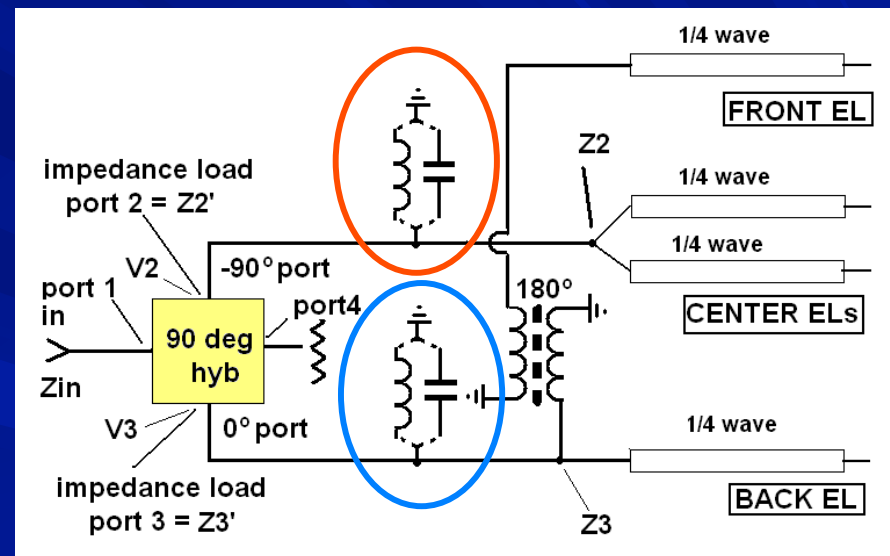
This is a method which, when applied, ensures the hybrid does exactly what we want

**Remember the trick:**

- turn **both** load impedances into **REAL** impedances by using parallel coil/cap
- correct the voltage magnitude by changing **fo**

# Demystifying the hybrid coupler

- Every complex impedance can be transformed to a real impedance by a **shunt reactance**
- $53.7 + j22.5$  in parallel with  $-j168.4$  gives a real  $Z2' = \mathbf{66.14 \Omega}$
- $60.7 - j36.1$  in parallel with  $+j138.2$  gives  $Z3 = \mathbf{82.17 \Omega}$
- Parallel reactances do NOT change the voltage magnitude! (same for element **drive current**)
- We developed **modeling software** that calculates these required parallel impedances



# Demystifying the hybrid coupler

## A special Modeling Tool

calculates the following data:

- $X_2$  (across  $Z_2$ ) =  $-150.7 \Omega$
  - $X_3$  (across  $Z_3$ ) =  $138.2 \Omega$
- to obtain resistive impedances  $Z_2'$  and  $Z_3'$  and  $\Delta\phi = 90^\circ$  :
- $Z_2' = 63.13 \Omega$
- $Z_3' = 82.05 \Omega$
- **New  $f_0$**  to obtain the desired k-value (in this case  $k = 1$ )

Also shown:

Dump power  
 $Z_{in}$  and SWR

HYBRID COUPLER OPTIMIZATION PHASE COMPENSATED DESIGN SYSTEM -w1mk -			
Enter data in yellow background cells		by W1MK - OH4UH	
CALCULATING THE SHUNT ELEMENTS			
1	Enter $f_a$ (design freq) array →	3.650	MHz
2	Enter k-value →	1	
		Real part	Imag part
3	(-90 ° branch) Enter $Z_2$ →	53.70	22.50 $\Omega$
4	Branch 2 shunt element →	-150.66 $\Omega$	←
5	→	289.42 pF	
6	$Z_2'$ (at port 2) →	63.13 $\Omega$	←
		Real part	Imag part
7	(0° branch) Enter $Z_3$ →	60.70	-36.00 $\Omega$
8	Branch 3 shunt element →	138.35 $\Omega$	←
9	→	6.03 $\mu\text{H}$	
10	$Z_3'$ (at port 3) →	82.05 $\Omega$	←
HYBRID INPUT DATA			
11	Enter $Z_0$ Hybrid →	50.0 $\Omega$	
OUTPUT DATA			
12	Frequency corr. factor =	1.1135	
13	New Hybrid $f_0$ =	4.064 MHz	
14	L-Hybrid =	1.36 $\mu\text{H}$	
15	C-Hybrd =	392 pF	
16	Dump port (port 4) power ratio =	-14.9 dB	
17	Real part $Z_{in}$ (port 1) =	49.29 $\Omega$	←
18	Imag. part $Z_{in}$ (port1) =	4.37 $\Omega$	←
19	Port 1 return loss (dB) =	27.1 dB	
20	Port 1 SWR =	1.09	←

# Demystifying the hybrid coupler

Check it with the hybrid model spreadsheet

HYBRID COUPLER OPTIMIZATION PHASE COMPENSATED DESIGN SYSTEM -w1mk -			
Enter data in yellow background cells		by W1MK - OH4UH	
CALCULATING THE SHUNT ELEMENTS			
1	Enter fa (design freq) array →	3.650	MHz
2	Enter k-value →	1	
		Real part	Imag part
3	(-90 ° branch) Enter Z2 →	53.70	22.50 Ω
4	Branch 2 shunt element →	-150.66	Ω
5	→	289.42	pF
6	Z2' (at port 2) →	63.13	Ω
		Real part	Imag part
7	(0° branch) Enter Z3 →	60.70	-36.00 Ω
8	Branch 3 shunt element →	138.35	Ω
9	→	6.03	uH
10	Z3' (at port 3) →	82.05	Ω
HYBRID INPUT DATA			
11	Enter Zo Hybrid →	50.0	Ω
OUTPUT DATA			
12	Frequency corr. factor =	1.1135	
13	New Hybrid fo =	4.064	MHz
14	L-Hybrid =	1.96	uH
15	C-Hybrd =	392	pF
16	Dump port (port 4) power ratio =	-14.9	dB
17	Real part Zin (port 1) =	49.29	Ω
18	Imag. part Zin (port1) =	4.37	Ω
19	Port 1 return loss (dB) =	27.1	dB
20	Port 1 SWR =	1.09	

HYBRID COUPLER DESIGN (by W1MK)			
INPUTS			
ENTER fa (operating frequency) →	3.65	MHz	
ENTER fo (hybrid frequency) →	4.064	MHz	
ENTER Zo Design impedance hybrid →	50	Ω	
	Real Part	Imag Part	
ENTER Impedance load PORT 2 (Z2) →	63.13	0	Ω
ENTER Impedance load PORT 3 (Z3) →	82.02	0	Ω
RESULTS			
fo/fa =	1.113		
Hybrid L value (uH) =	1.96	μH	
Hybrid C value (pF) =	392	pF	
Ratio Voltage magnitude Port2/Port3 (k) =	1.000		
Phase angle Voltage port 2 vs. port 3 =	90.00	°	
Power in Port 4 (vs. Pwr in Port 1) =	-14.9	dB	
Real part input impedance (port 1) =	49.34	Ω	
Imaginary part input impedance (port1) =	4.35	Ω	
Return loss (port 1) =	-27.1	dB	
SWR =	1.09		

# Demystifying the hybrid coupler

HYBRID COUPLER DESIGN (by W1MK)			
INPUTS			
ENTER fa (operating frequency) →	3.65	MHz	
ENTER fo (hybrid frequency) →	3.65	MHz	
ENTER Zo Design impedance hybrid →	50	Ω	
	Real Part	Imag Part	
ENTER Impedance load PORT 2 (Z2) →	53.7	22.5	Ω
ENTER Impedance load PORT 3 (Z3) →	60.7	-36.1	Ω
RESULTS			
fo/fa =	1.000		
Hybrid L value (uH) =	2.18	μH	
Hybrid C value (pF) =	436	pF	
Ratio Voltage magnitude Port2/Port3 (k) =	0.905		
Phase angle Voltage port 2 vs. port 3 =	-66.83	°	
Power in Port 4 (vs. Pwr in Port 1) =	-17.1	dB	
Real part input impedance (port 1) =	79.78	Ω	
Imaginary part input impedance (port1) =	8.84	Ω	
Return loss (port 1) =	-12.4	dB	
SWR =	1.63		

HYBRID COUPLER DESIGN (by W1MK)			
INPUTS			
ENTER fa (operating frequency) →	3.65	MHz	
ENTER fo (hybrid frequency) →	4.064	MHz	
ENTER Zo Design impedance hybrid →	50	Ω	
	Real Part	Imag Part	
ENTER Impedance load PORT 2 (Z2) →	63.13	0	Ω
ENTER Impedance load PORT 3 (Z3) →	82.02	0	Ω
RESULTS			
fo/fa =	1.113		
Hybrid L value (uH) =	1.96	μH	
Hybrid C value (pF) =	392	pF	
Ratio Voltage magnitude Port2/Port3 (k) =	1.000		
Phase angle Voltage port 2 vs. port 3 =	-90.00	°	
Power in Port 4 (vs. Pwr in Port 1) =	-14.9	dB	
Real part input impedance (port 1) =	49.34	Ω	
Imaginary part input impedance (port1) =	4.35	Ω	
Return loss (port 1) =	-27.1	dB	
SWR =	1.09		

Without shunt elements

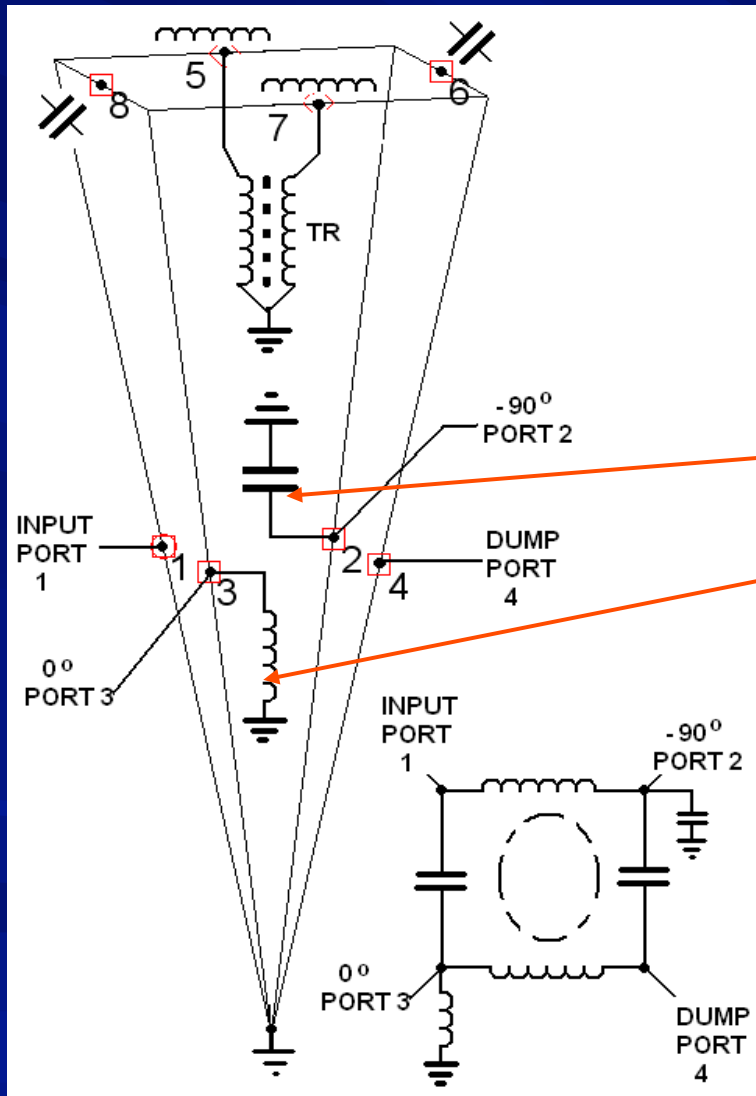
With shunt elements

# *Demystifying the hybrid coupler*

■ And now the moment of truth..

- To do **bandwidth assessment** ...
- ... we will run the EZNEC model in **Sweep mode** (across the band)
- ... we require a model that includes the hybrid
- and all other antenna system elements

# Demystifying the hybrid coupler



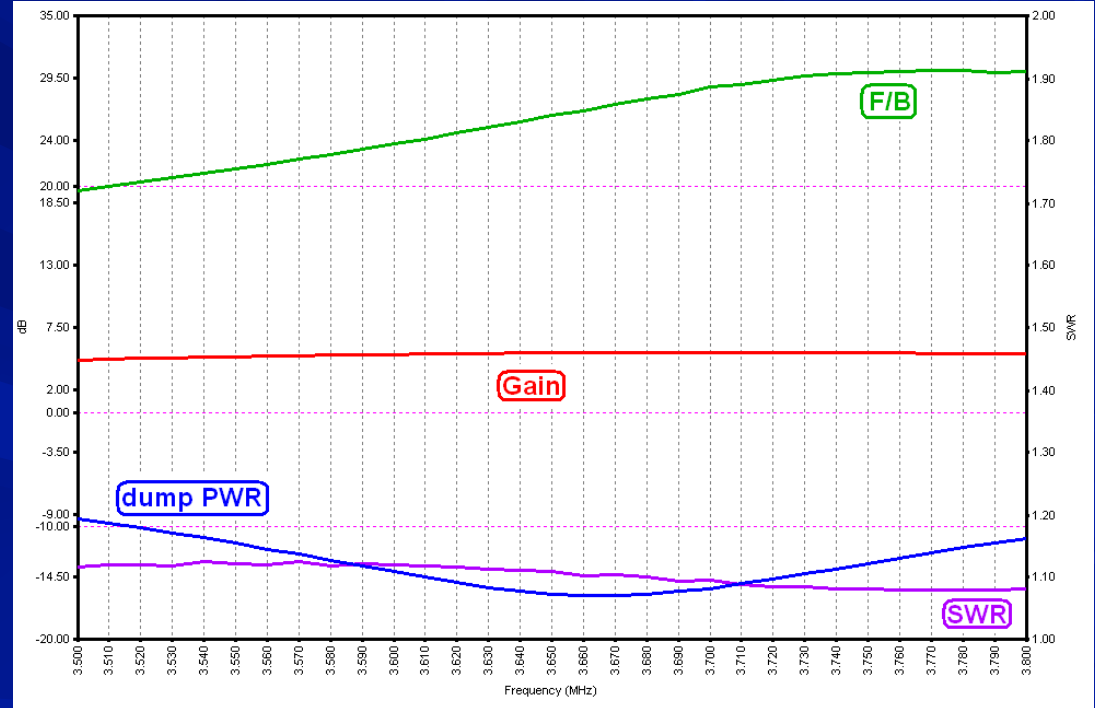
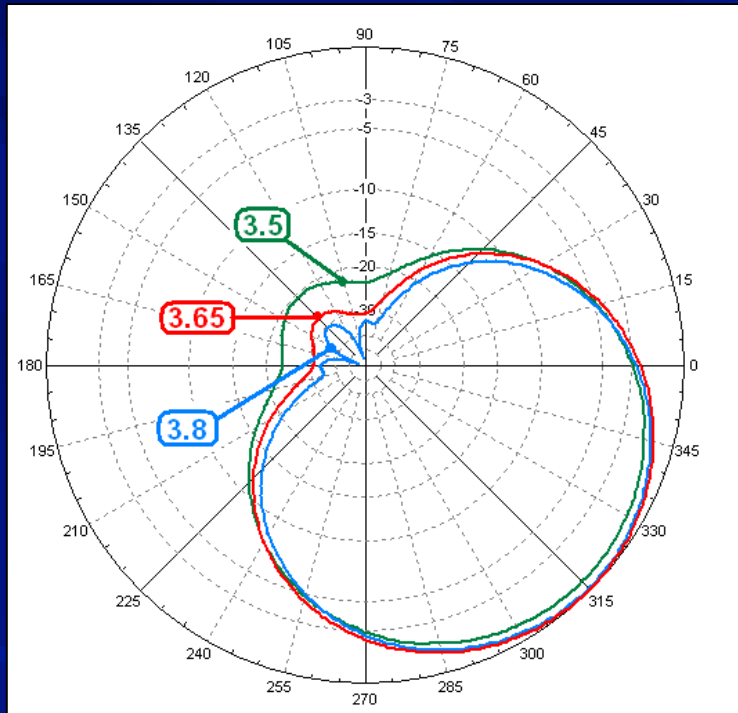
## BANDWIDTH ASSESSMENT

Wire #	Specified Pos. % From E1	Actual Pos. % From E1	Seg	R (ohms)	L (uH)	C (pF)
1	50	50	2	0.01	Short	Short
2	50	50	2	100000	Open	289.4
3	50	50	2	100000	6	Open
4	50	50	2	50	Short	Short
5	50	50	2	Short	1.958	Short
6	50	50	2	Short	Short	391.6
7	50	50	2	Short	10000	Short
8	50	50	2	Short	Short	391.6

The EZNEC model now includes the hybrid **and** the shunt elements

# Demystifying the hybrid coupler

## Operational Bandwidth for W1MK's 2-shunt method



COMPARE WITH  
SLIDE 10



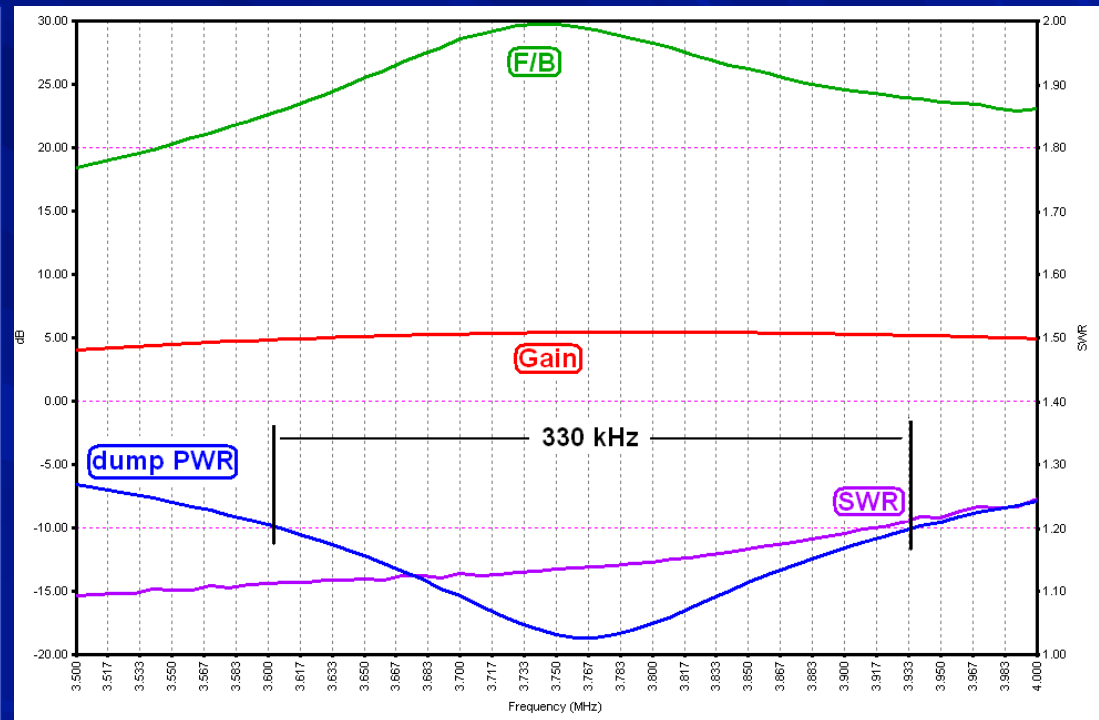
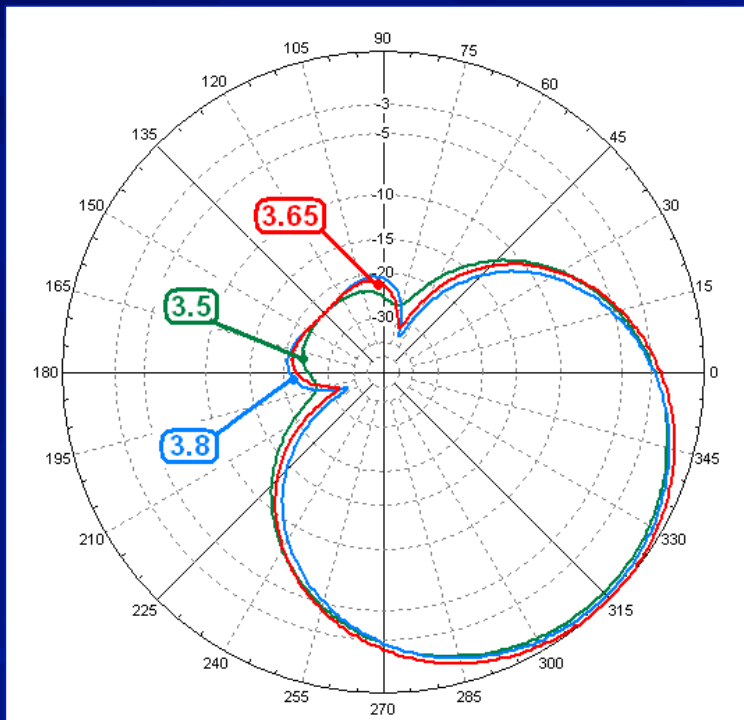
# *Demystifying the hybrid coupler*

There are two other methods

- The W1MK **single shunt** method
- The W8WWV double network system

# Demystifying the hybrid coupler

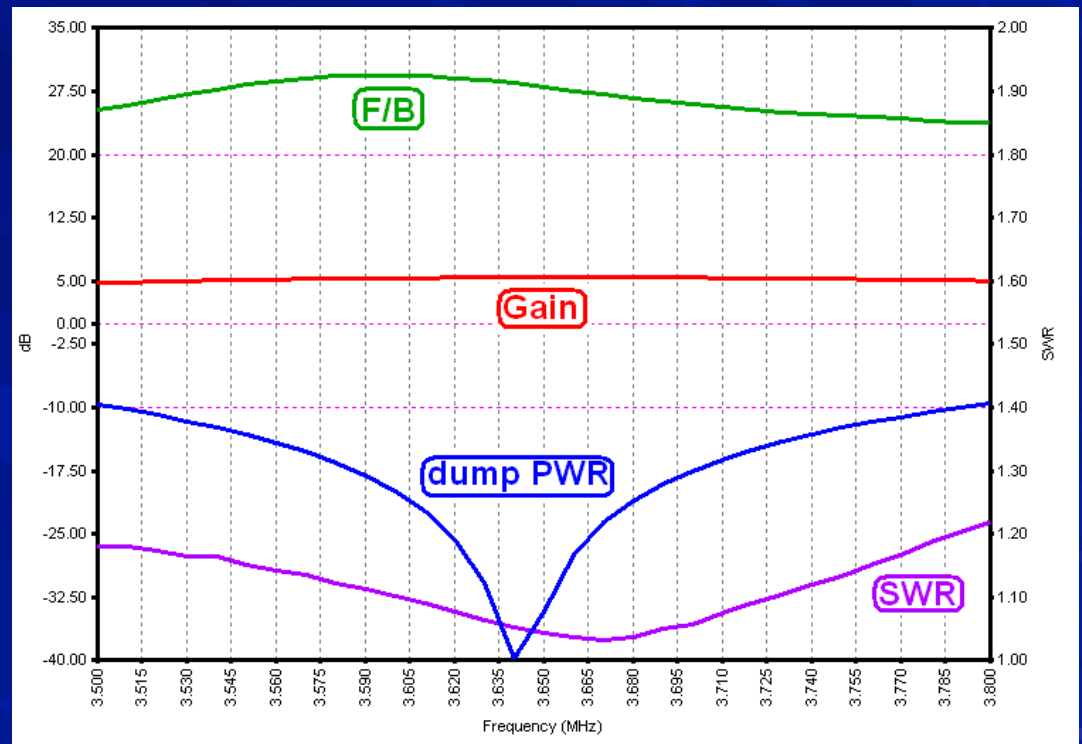
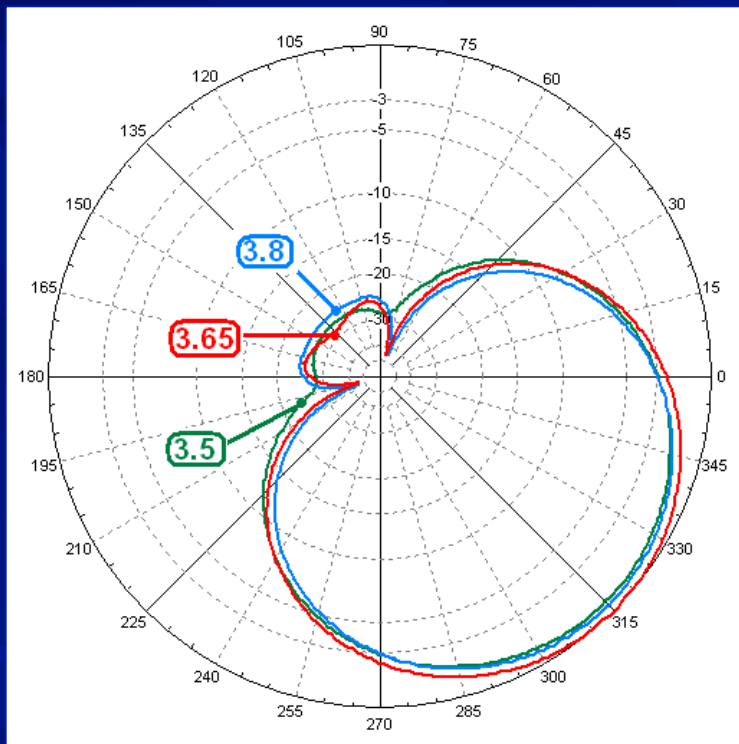
## Operational Bandwidth for W1MK's **single shunt method**



COMPARE WITH  
SLIDE 10

# Demystifying the hybrid coupler

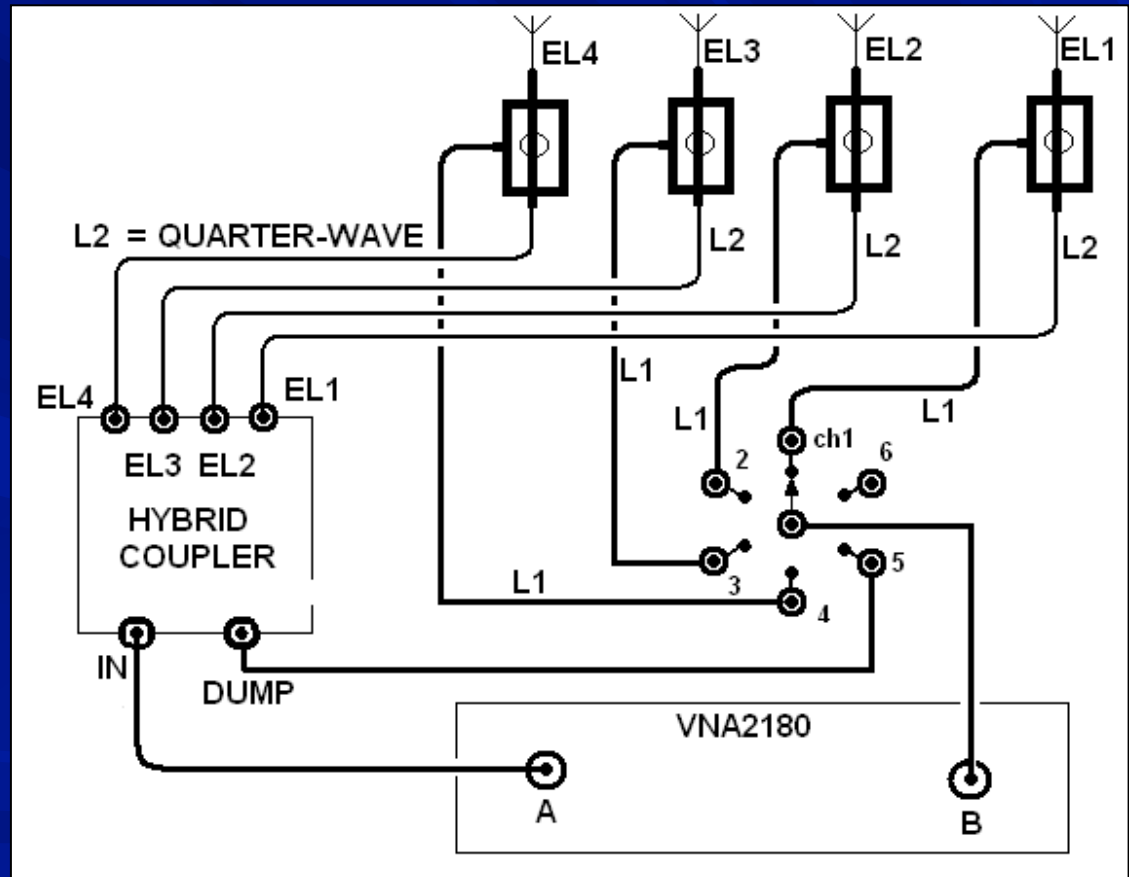
## W8WWV's double network system



# Demystifying the hybrid coupler



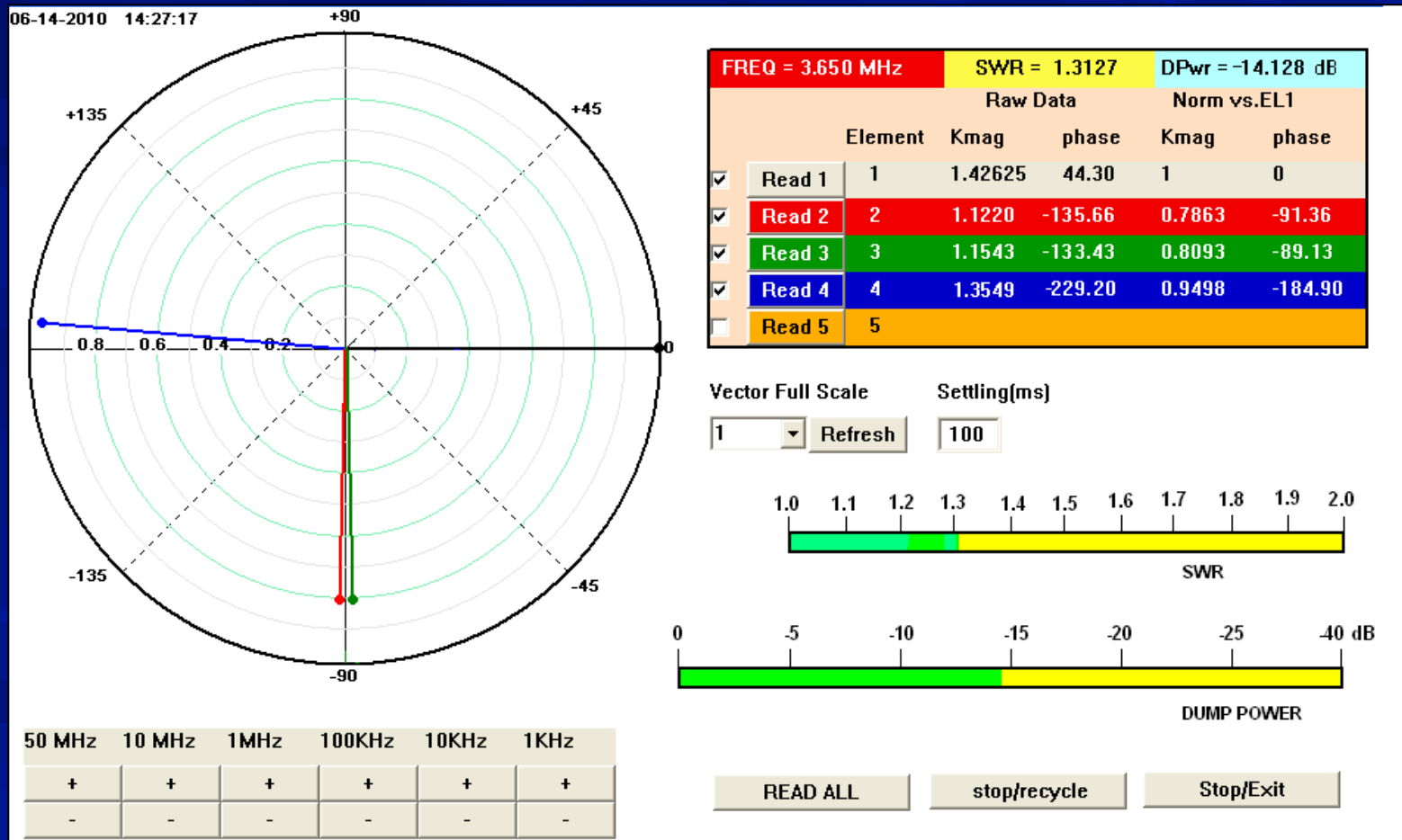
## Measuring / testing



VNA + MUX + PROBES

# Demystifying the hybrid coupler

## RVM (Relative Vector Meter) setup



Real Time (single frequency)

# *Demystifying the hybrid coupler*

## Conclusion

- No more mysterious properties for a hybrid
- For the first time a complete and simple hybrid model
- A hybrid can be modeled **in** EZNEC
- Operational BW: **L-netw. 4-sq: 75 kHz, hybrid: 300 kHz**
- The new 2-port black box Z2 – Z3 approach
- Ways to measure / calculate Z2 and Z3
- **Three optimization methods** turning the hybrid coupler fed array into a very high performance wideband (300 kHz on 80m) antenna system
- Modeling software for each method
- Very handy LBDXView program from W8WWV
- VNA + MUX for final verification

ON4UN's Low-Band DXing



Devoldere

Fifth Edition



ON4UN's

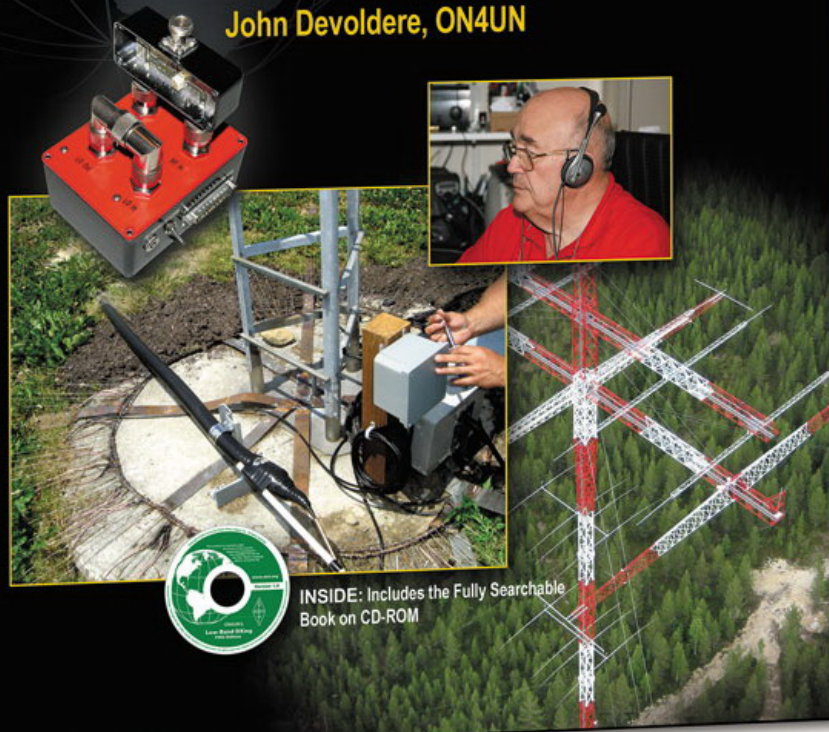


# Low-Band DXing

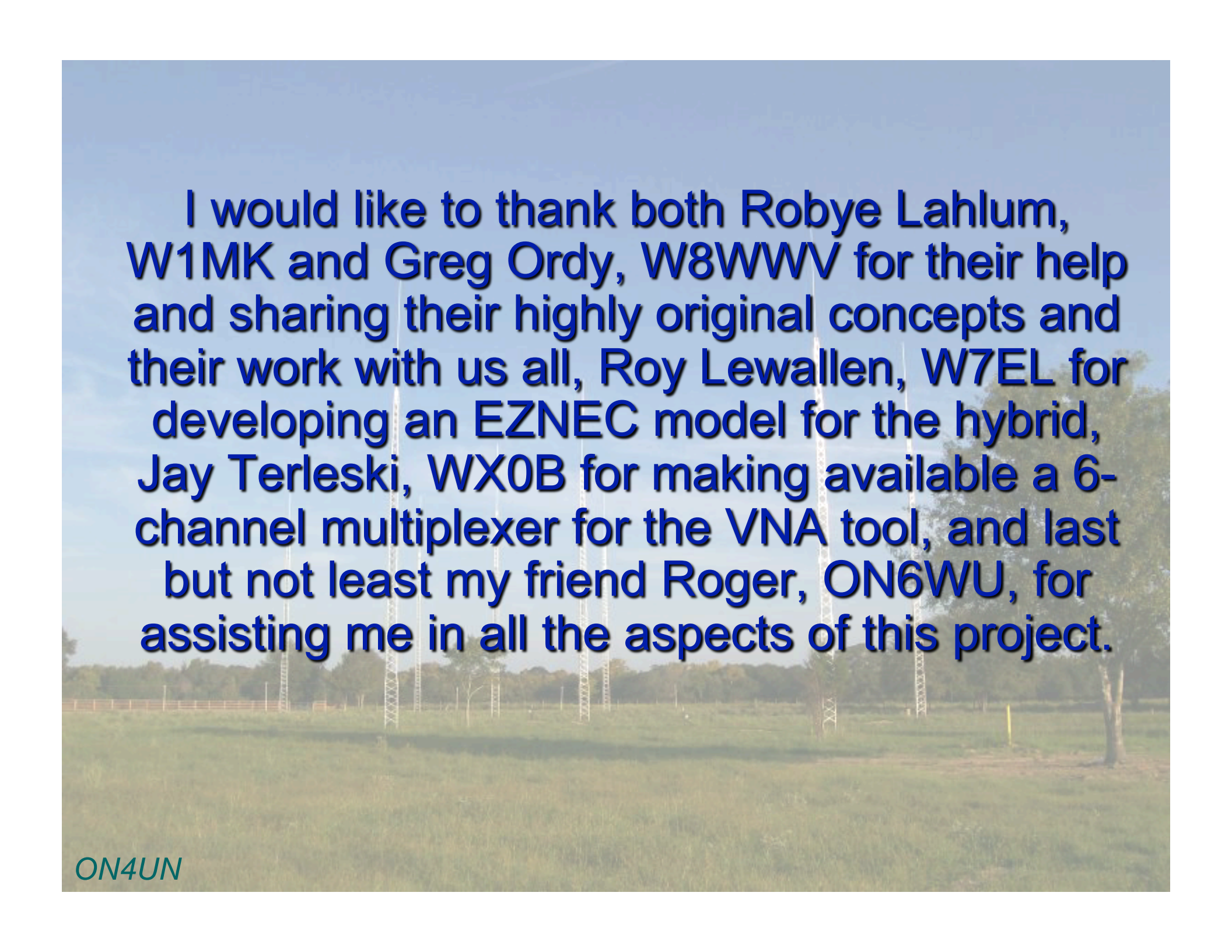
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John Devoldere, ON4UN



INSIDE: Includes the Fully Searchable  
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I would like to thank both Robye Lahlum, W1MK and Greg Ordy, W8WWV for their help and sharing their highly original concepts and their work with us all, Roy Lewallen, W7EL for developing an EZNEC model for the hybrid, Jay Terleski, WX0B for making available a 6-channel multiplexer for the VNA tool, and last but not least my friend Roger, ON6WU, for assisting me in all the aspects of this project.



4-squares at NR5M

*Thank you  
for listening !*

